

M.Sc. III Semester Degree Examination, April/May - 2024

MATHEMATICS

Computational Techniques

(NEP)

Time : 3 Hours

Maximum Marks : 70

Note : Answer **any five** of the following questions with Question No. **1 (Q.1)** is **Compulsory**.
Each question carries **equal** marks.

1. (a) With the usual notation derive the Newton-cotes formula and hence derive Simpsons one third formula. **5**
- (b) A tank is discharging water through an orifice at a depth of 'x' metres below the surface of the water whose area is 'Am²'. The following are the table of 'x' for corresponding value of 'A'. **5**

A	1.257	1.39	1.52	1.65	1.809	1.962	2.123	2.295	2.462	2.65	2.827
x	1.50	1.69	1.80	1.95	2.10	2.25	2.40	2.55	2.70	2.85	3.00

Using the formula (0.018) $T = \int_{1.5}^3 \frac{A}{\sqrt{x}} dx$,

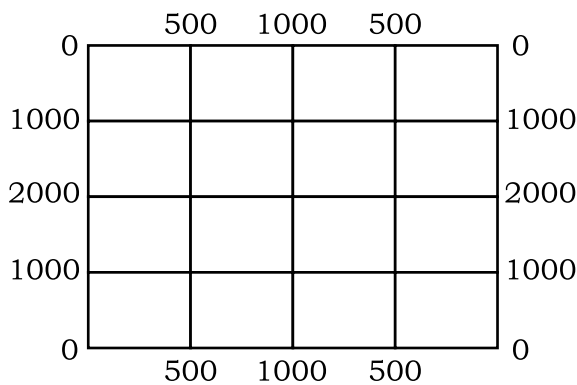
Calculate 'T' the time in seconds for the level of the water to drop 3.0 m to 1.5 m above the orifice.

- (c) Evaluate the approximate value of the integral $\int_2^4 \frac{e^x}{\sin x + x} dx$ by using. **4**
- (i) Gauss-Chebyshev three point formula
- (ii) Gauss-Legendre three point formula
2. (a) Define initial value problem. Discuss the Taylor series method to find the numerical solution of the ODE $\frac{dy}{dx} = f(x, y); y(x_0) = y_0$. **7**
- (b) Using Modified Euler's method. Compute $y(0.2)$ from $\frac{dy}{dx} = x + y; y(1) = 2$ taking step size $h = 0.1$. Compare the results obtained by this method with the results obtained by analytical method. **7**

3. (a) Discuss the Milne's Predictor-Corrector method to find the numerical solution of the differential equation. **10**

$$\frac{dy}{dx} = f(x, y); y(x_0) = y_0$$

- (b) Using Galerkin Method solve the following BVP described by the differential equation $u'' + u + x = 0$, $0 < x < 1$ subjected to the boundary conditions $u(0) = u(1) = 0$. **4**
4. (a) Solve the Elliptic equation $u_{xx} + u_{yy} = 0$ for the square mesh of the figure with boundary value as shown. **7**



- (b) Solve the PDE $\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2}$ subjected to the boundary condition. **7**
 $u(x, 0) = \sin \pi x$, $0 \leq x \leq 1$; $u(0, t) = u(1, t) = 0$. Carry out computation's for two levels, taking $h = \frac{1}{3}$ and $k = \frac{1}{36}$.
5. (a) Fit the least square for the curve $y = ax^3$ with the following data and hence estimate 'y' at $x = 6$ **7**

x	1	2	3	4	5
y	0.5	2	4.5	8	12.5

- (b) Explain the non-linear regression with an example. **7**
6. Using Euler's method. Find the value of $y(0.1)$, $y(0.2)$ and $y(0.3)$ for **14**

$$\frac{dy}{dx} = xy + y^2; y(0) = 1.$$

Hence find the value of $y(0.3)$ by using Adams-Bashforth-Moulton method.



7. (a) Explain the Liebmann's iteration process for solving Laplace equation. **7**
- (b) Fit the normal equations and hence find the best fit value of x , y and z in the Least square sense from the following equations. **7**
- $$x + 2y + z = 1;$$
- $$2x + y + z = 4;$$
- $$-x + y + 2z = 4;$$
- $$4x + 2y - 5z = -7.$$
8. (a) Explain the stability of Runge-Kutta method. **5**
- (b) Explain the shooting technique for numerical solution of the BVP for ordinary differential equation. **5**
- (c) Discuss the classification of Partial differential equation. **4**

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