21BCA1C3MFL(46143)

B.C.A. I Semester Degree Examination, April/May - 2024 COMPUTER SCIENCE

Mathematical Foundation

(NEP)

Time : 2 Hours

Maximum Marks: 60

SECTION - A

Answer the following sub-questions. Each sub-question carries one mark. 10x1=10

- (a) Write the negation of the following statement "The sum of 3 and 4 is 9".
 - (b) Check whether the following sentence is statement "There are 35 days in a month".

(c) Find adjoint of matrix
$$\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$$

(d) Find the Rank of the following matrix
$$\begin{vmatrix} 1 & 1 & 3 \\ 0 & 2 & -6 \\ 0 & 0 & 4 \end{vmatrix}$$
.

(e) Find the degree measure to radian $\frac{5\pi}{3}$.

- (f) Find $\tan x$, if $\cot x = \frac{3}{4}$ lies in third quadrant.
- (g) Evaluate : $\lim_{x \to 2} \frac{x+1}{x-1}$
- (h) Differentiate $x^2 + 3x + 2$ w.r.t x.

(i) Evaluate :
$$\int_{0}^{2} x^{7} dx$$

(j) Evaluate : $\int 4x^3 - 6 \, dx$

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SECTION - B

Answer **any four** of the following questions. Each question carries **five** marks.

- 2. Prove the following by truth table $\sim (p \Rightarrow q) = \sim (\sim p \lor q)$.
- **3.** Find the Inverse of a matrix $A = \begin{bmatrix} 2 & -2 \\ 4 & 3 \end{bmatrix}$.
- **4.** Prove that

$$\sin^2\frac{\pi}{6} + \cos^2\frac{\pi}{3} - \tan^2\frac{\pi}{4} = \frac{-1}{2}$$

- 5. Evaluate : $\lim_{x \to 2} \frac{3x^2 x 10}{x^2 4}$
- **6.** Evaluate : $\int x \cos x \, dx$
- 7. State and verify the property 1 of determinants $\begin{vmatrix} 2 & -3 & 5 \\ 6 & 0 & 4 \\ 1 & 5 & -7 \end{vmatrix}$.

SECTION - C

Answer any three of the following questions. Each question carries ten marks.

3x10=30

- (a) Define contradiction with example.
 - (b) Show that the proposition $(p \lor q) \land (\neg p \land \neg q)$ is a contradiction.
- **9.** Solve the following by Cramer's rule.
 - x+y+z=6 x-y+z=22x+y-z=1
- **10.** If $\cos x = \frac{-1}{2}$ where x lies in 3rd quadrant then find all the remaining trignometric ratios.
- 11. Differentiate :

8.

- (a) $\sin(x^2 + 5)$ w.r.t. *x*.
- (b) Differentiate : $x^2 \sin x$ w.r.t. x.

12. Evaluate :
$$\int_{0}^{2} \int_{1}^{3} xy^2 \, \mathrm{d}y \, \mathrm{d}x$$

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4x5=20